

AD-A250 581



ITION PAGE

Form Approved
OMB No. 0704-0188

Average 1 hour per response, including the time for reviewing instructions, searching existing data sources, gathering and maintaining the data needed, and completing and reviewing the collection of information. Send comments regarding the burden estimate or any other aspect of the collection of information to Washington Headquarters Services, Directorate for Information Operations and Reports, 1215 Jefferson Management and Budget, Paperwork Reduction Project (0704-0188), Washington, DC 20583.

1. AGENCY USE ONLY (Leave blank)	2. REPORT DATE	3. REPORT TYPE AND DATES COVERED	
		Final Report 1 Nov 90-31 Oct 91	
4. TITLE AND SUBTITLE		5. FUNDING NUMBERS	
Statistical Mechanics of Collective Phenomena in Plasmas		AFOSR-87-0010	
6. AUTHOR(S)			
Professor Joel. L. Lebowitz			
7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES)		8. PERFORMING ORGANIZATION REPORT NUMBER	
Dept of Physics Hill Center Center Rutgers University New Brunswick, NJ 08903		AFOSR-TR- 92 0277	
9. SPONSORING/MONITORING AGENCY NAME(S) AND ADDRESS(ES)		10. SPONSORING/MONITORING AGENCY REPORT NUMBER	
AFOSR/NE Bldg 410 Bolling AFB DC 20332-6448 Dr Barker		2301/ES	
11. SUPPLEMENTARY NOTES			
<p style="text-align: center;">DTIC ELECTED MAY 26 1992</p>			
12. DISTRIBUTION/AVAILABILITY STATEMENT			
UNLIMITED			
13. ABSTRACT (Maximum 200 words)			
<p>We have carried out theoretical studies of equilibrium and non-equilibrium properties of strongly coupled particle systems, and of the phenomena which take place when neutral or partially ionized atoms interact strongly with external fields and with each other in a plasma. The main tools of our study are statistical mechanics and kinetic theory, including the transition from a microscopic to a hydrodynamic description. Quantum mechanics plays a central role in many of these problems, and is an important ingredient in our work.</p>			
<div style="border: 1px solid black; padding: 5px;"> This document has been approved for public release and sale; its distribution is unlimited. </div>			
14. SUBJECT TERMS		15. NUMBER OF PAGES	
17. SECURITY CLASSIFICATION OF REPORT		18. SECURITY CLASSIFICATION OF THIS PAGE	
UNCLASS		UNCLASS	
19. SECURITY CLASSIFICATION OF ABSTRACT		20. LIMITATION OF ABSTRACT	
UNCLASS		UL	

NSN 7540-01-280-5500

Standard Form 298 (890104 Draft)
Prescribed by ANSI Std. Z39-18
1984

TECHNICAL REPORT
AFOSR GRANT 87-0010

STATISTICAL MECHANICS OF COLLECTIVE PHENOMENA IN PLASMAS

NOVEMBER 1, 1990 - OCTOBER 31, 1991

Accesion For	
NTIS	CRA&I
DTIC	TAB
Unannounced	
Justification	
By _____	
Distribution /	
Availability Codes	
Dist	Aval and/or Special
A-1	

by
Joel L. Lebowitz
Professor of Mathematics and Physics
Hill Center
Rutgers University
New Brunswick, NJ 08903
Principal Investigator



92-13057



92 5 15 027

ABSTRACT

We have carried out theoretical studies of equilibrium and non-equilibrium properties of strongly coupled particle systems, and of the phenomena which take place when neutral or partially ionized atoms interact strongly with external fields and with each other in a plasma. The main tools of our study are statistical mechanics and kinetic theory, including the transition from a microscopic to a hydrodynamic description. Quantum mechanics plays a central role in many of these problems, and is an important ingredient in our work.

1. ELECTRON VELOCITY DISTRIBUTION IN A WEAKLY IONIZED PLASMA WITH AN EXTERNAL ELECTRIC FIELD

We consider a weakly ionized gas in the presence of an externally imposed spatially homogeneous electric field E which may be either constant or vary in time. The density of the gas, the degree of ionization and the strength of the field are assumed to be such that: (i) the interactions between the electrons and of the electrons with the ions and neutrals can be described by Boltzmann type elastic collision integrals and, (ii) collisions between the electrons and the heavy components of the plasma, ions and neutrals, are adequately described by assuming the latter to be in a Maxwellian distribution with a priori given temperatures. Under these assumptions the time evolution of the spatially homogeneous electron velocity distribution function $f(v, t)$ will satisfy the Boltzmann equation

$$\frac{\partial f}{\partial t} - (e/m)E \cdot \nabla f = (L_i + L_n)f + Q(f, f). \quad (1.1)$$

The right side of (1.1) consists of a linear part corresponding to elastic collisions

between the electrons and the heavy components (ions and neutrals) and a quadratic Landau type collision integrals for e-e interactions.

Eq. (1.1) differs from the frequently studied linear kinetic equation for an essentially zero density "electron swarm" by the omission of inelastic e-n collisions and the inclusion of elastic e-i and e-e collisions. It also differs from the strongly coupled plasma case in that we neglect collective plasma interactions.

We find that (in the approximation scheme used) this equation has for a stationary f (in a constant field), non-unique solutions for a certain range of E , in agreement with that found by us in earlier investigations. We interpret these to correspond to hysteresis effects when the field is changing very slowly indicating a very sharp changeover, possibly a discontinuous transition, in the stationary state of the electrons at a certain critical E . Possible applications of this effect are being investigated.

2. NEGATIVE TEMPERATURE STATES AND EQUIVALENCE OF ENSEMBLES FOR THE VORTEX MODEL OF TWO-DIMENSIONAL TURBULENCE

We studied Onsager's theory of large, coherent vortices in turbulent flows in the approximation of the point-vortex model for two-dimensional Euler hydrodynamics. In the limit of a large number of point vortices with the energy per pair of vortices held fixed, we prove the entropy defined from the microcanonical distribution as a function of the (pair-specific) energy has its maximum at a finite value and thereafter decreases, yielding the negative-temperature states predicted by Onsager. We furthermore show that the equilibrium vorticity distribution maximizes an appropriate entropy functional subject

to the constraint of fixed energy, and, under regularity assumptions, obeys the Joyce-Montgomery mean-field equation. We also prove that, under appropriate conditions, the vorticity distribution is the same as that for the canonical distribution, a form of equivalence of ensembles. We also establish a large fluctuation theory for the microcanonical distributions, which is based on a level-3 large deviations theory for exchangeable distributions. We discuss some implications of that property for the ergodicity requirements to justify Onsager's theory, and also the theoretical foundations of a recent extension to continuous vorticity fields by R. Robert and J. Miller.

Although the theory of two-dimensional vortices is of primary interest, our proofs actually apply to a very general class of mean-field models with long-range interactions in arbitrary dimensions.

3. QUANTUM PARTICLE IN AN ELECTRIC FIELD

The Einstein-Kubo relation between the diffusion constant D and the linear mobility ν was investigated for a dissipative quantum particle in a potential $V(x) = -Ex + V_0 \cos(k_0 x)$. This system is directly related to a current biased Josephson junction. It is shown that $D = kT\nu$ holds to all order in V_0 provided the dissipation spectrum $J(\omega)$ is linear near $\omega \rightarrow 0$ and is not pathological. A generalized version of the Einstein relation is shown to hold also for sub-Ohmic dissipation, $J(\omega) \sim \omega^s$, $0 < s < 1$, as $\omega \rightarrow 0$ where the motion is sub-diffusive. The super-Ohmic case $1 < s < 2$ was also studied.

We further obtained an analytic expression for the nonlinear mobility of a quantum particle moving down a cosine potential in the presence of a finite bias force in the small viscosity limit. This is used to explain some experimental

observations on Josephson junctions in which the Coulomb blockade is important. The result is based on a resummation of a series expansion of the mobility in V_0 (the strength of the cosine potential) and is applicable to a variety of regimes in the parameter space.

4. FLOQUET SPECTRUM FOR TWO-LEVEL SYSTEMS IN QUASIPERIODIC TIME DEPENDENT FIELDS

We studied the time evolution of N-level quantum systems under quasiperiodic time dependent perturbations. The problem is formulated in terms of the spectral properties of a quasienergy operator defined in an enlarged Hilbert space, or equivalently of a generalized Floquet operator. We discuss criteria for the appearance of pure point as well as continuous spectrum, corresponding respectively to stable quasiperiodic dynamics and to unstable chaotic behavior. We discuss two types of mechanisms that lead to instability. The first one is due to near resonances, while the second one is of topological nature and can be present for arbitrary ratios between the frequencies of the perturbation. We treat explicitly an example of this type. The stability of the pure point spectrum under small perturbations is proven using KAM techniques.

LIST OF PUBLICATIONS FROM GRANT

Quenching Einstein Coefficients in Plasmas, Physical Review A, 41, 4, 2127–2137 (1990), (with Y.-C. Chen)

Dissipation and Large Thermodynamic Fluctuations, Jour. Stat. Phys., 61, 533–572, (1990), Gregory L. Eyink

Time-dependent Statistical Properties of the Electric Microfield Seen by a Neutral Radiator, Physical Review A, 43, 2673–2693, (1991), (with A. Alastuey and D. Levesque)

Diffusive Energy Growth in Classical Quantum Driven Oscillators, Jour. Stat. Phys., 62, 793–817, (1991), (with L. Bunimovich, H.R. Jauslin, A. Pellegrinotti and P. Nielaba)

The Electron Component of a Plasma in a Homogeneous Electric Field, Physical Review A, 43, 4438–4451, (1991), Alexander V. Rokhlenko

Spectral and Stability Aspects of Quantum Chaos, Chaos, (1991), (with H.R. Jauslin)

Driven Diffusive Systems with a Moving Obstacle: A Variation on the Brazil Nuts Problem, J. Phys. A, L375, (1990), (with Francis J. Alexander)

Coulomb Field of an Accelerated Charge, submitted to Physical Review D, Francis J. Alexander and V.H. Gerlach

Electron Distribution in a Weakly Ionized Plasma in an External Electric Field, (with A. Rokhlenko), in preparation

Quantum Particle in a Washboard Potential – Part I: Linear Mobility and the Einstein Relation, with Y.C. Chen, preprint

Quantum Particle in a Washboard Potential – Part II: Nonlinear Mobility and the Josephson Junction, with Y.C. Chen, preprint

Atomic versus Ionized States in Many Particles Systems and the Spectra of Reduced Density Matrices: A Model Study, to appear in the Journal of Statistical Physics, (with N. Macris and P.A. Martin)

Spectral Properties of Quasiperiodically Driven Quantum Systems, to appear in Proceedings of the Locarno Conference, (with H. Jauslin)